EPPS 6313 : Recitation Session #2

Problem 1

By using the IQ example below, with a population average = 100 and population standard deviation = 15, Calculate the probability that a randomly selected person would have :

- 1. An IQ of 115 or more
- 2. An IQ between 100 and 120
- 3. An IQ between 80 and 90
- $4.\ \, {\rm An~IQ}$ between 70 and 100

Problem 2

If a random sample of size n=20 from a normal population with the variance $\sigma^2=225$ has the mean $\bar{x}=64.3$, construct a 95% confidence interval for the population mean μ

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EPPS 6316 : Recitation Session #2

Problem 1

For the simple regression $Y_i = \beta_1 + \beta_2 X_i + u_i$, verify the following numerical properties of the OLS estimators:

$$\sum e_i \hat{Y}_i = 0$$

$$\sum \hat{Y}_i = \sum Y_i$$

Problem 2

Show
$$cov(\hat{\beta}_1, \hat{\beta}_2) = -\bar{X}var(\hat{\beta}_2) = -\sigma^2 \frac{\bar{X}}{\sum x_i^2}$$