

I . Short Review

1. Z score

- $Z = \frac{X-\mu}{\sigma}$, $\frac{X-\bar{X}}{s}$

$\therefore X = \mu + Z\sigma$, $\bar{X} + Zs$

- Look at the table in your textbook. ((b) and (c) column) ; Proportions are not percentages.
- $\Pr(x \geq a)$, $\Pr(a \leq x \leq b)$, What value in 95% , 95 percentile and etc. : to be covered in session

2. Sampling Distribution of Means

- $\mu_{\bar{x}}$: Sample mean is average of means ($\bar{X}_1, \bar{X}_2, \bar{X}_3, \dots$)
- Three properties : ① the sampling distribution of means approximates the normal curve. (the central limits theorem, $n \geq 30$) ② $\mu_{\bar{x}} = \mu$ ③ $\sigma_{\bar{x}}$ (or standard error of \bar{X}) $< \sigma$: $\sigma_{\bar{x}} = \frac{\sigma}{\sqrt{n}}$, $\hat{\sigma}_{\bar{x}} (s_{\bar{x}}) = \frac{s}{\sqrt{n}}$ (not n-1)
- $Z = \frac{X - \mu_{\bar{x}}}{\sigma_{\bar{x}}} = \frac{X - \mu_{\bar{x}}}{\frac{\sigma}{\sqrt{n}}}$
- Sample size : if $n \geq 30$, normal distribution. We can use Z score
However, if $n < 30$, we should use “(student) t-distribution”
: Look at the table. α : level of significance.(0.5), df : degree of freedom : n-1.

3. Confidence Interval

- CI : $\bar{X} \pm Z(\text{or } t)\sigma_{\bar{x}}$: For 95% confidence interval, $Z = 1.96$
For t score, look for t score in the table.
- $n \uparrow \rightarrow \sigma_{\bar{x}} \downarrow$ / $\sigma_{\bar{x}} \uparrow \rightarrow \text{CI} \uparrow$

| | Obs | Mean | Variation | Standard deviation |
|-----------------------------|-----------|-----------------|----------------------|--------------------|
| Sample | X | \bar{X} | s^2 | s |
| Population | X | μ | σ^2 | σ |
| Distribution of Sample mean | \bar{X} | $\mu_{\bar{x}}$ | $\sigma_{\bar{x}}^2$ | $\sigma_{\bar{x}}$ |

II. Problems

<Examples in Lecture Note>

(1) Using the IQ example, with a population average =100 and population standard deviation =15, calculate the probability that a randomly selected person would have:

1. An IQ of 115 or more
2. An IQ between 110 and 120
3. An IQ between 80 and 90
4. An IQ between 70 and 100

- The probability that randomly selected 2 people, having IQ of 110 or more. (each selection is independent).

(2) Using the assumptions that the true mean of hourly wage for UTD students is \$6, with a standard deviation of \$0.50, what is the probability of the following events:

1. Finding a sample mean of \$7 or more with a sample size of 25
2. Finding a sample mean of \$7 or more with a sample size of 100
3. Finding a sample mean of between \$4.50 and \$5.50 with a sample size of 100?

<Session Problem>

- (1) Test scores' population variance is 25, and random sample of 50 produced a mean of 82
- Find a 90% confidence interval
 - We just have 25 observations with $\sum f(x - \bar{x})^2 = 384$, but this is not population. Sample mean is 82. Find a 95% confidence interval.